

**Department of Communications
Engineering**

Communication Systems

Third Year Class

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Lecture 15

**Super heterodyne Receivers IV,
Image Rejection Ratio**

Image Rejection Ratio

Image Rejection Ratio (IRR) is dependent on the circuitry of the tuned circuit.

$$IRR = \alpha = \sqrt{1 + Q^2 \rho^2}$$

where Q is the tuned circuit quality factor, ρ can be calculated from

$$\rho = \frac{f_m}{f_c} - \frac{f_c}{f_m}$$

some references use f_{si} for f_m

* In the receiver, there is an RF-stage which has a tuned circuit.

* Further, in the mixer, there is another tuned circuit which also can reject image frequency.

* The overall IRR α is the product of both:-

$$\alpha_{total} = \alpha_{RF} \cdot \alpha_{MIXER}$$

Q/ A superheterodyne receiver having no RF amplifier, the Q of the antenna coupling circuit (at the input of the mixer) is 90.

Calculate:

① $F_{im} \approx IRR(\alpha)$ at $f_c = 950 \text{ KHz}$.

② $F_{im} \approx IRR(\alpha)$ at $f_c = 10 \text{ MHz}$.

③ what do you conclude?

Solution ① $Q = 90$, $F_{IF} = 455 \text{ KHz}$, $f_c = 950 \text{ KHz}$.

$$F_{im} = f_c + 2F_{IF} = 950 + 2 \times 455 = 1860 \text{ KHz}$$

$$\rho = \frac{F_{im}}{f_c} - \frac{f_c}{F_{im}} = \frac{1860}{950} - \frac{950}{1860} \approx 1.447$$

$$\alpha = \sqrt{1 + 90^2 (1.447)^2} \approx 130.247$$

② $Q = 90$, $F_{IF} = 455 \text{ KHz} = 0.455 \text{ MHz}$, $f_c = 10 \text{ MHz}$.

$$F_{im} = f_c + 2F_{IF} = 10 + 2 \times 0.455 = 10.91 \text{ MHz}$$

$$\rho = \frac{F_{im}}{f_c} - \frac{f_c}{F_{im}} = \frac{10.91}{10} - \frac{10}{10.91} = 1.091 - 0.91659 \approx 0.1744$$

$$\alpha = \sqrt{1 + 90^2 (0.1744)^2} \approx 15.729$$

③ We conclude that at low frequencies, IRR or the image can be rejected better than at high frequencies.

EX. 1 For a broadcast superheterodyne AM receiver having no RF amplifier, the Loaded Quality factor Q of the antenna coupling circuit is 100. Having $f_{IF} = 455 \text{ kHz}$, Find:

- ① the f_{im} and its rejection ratio at a carrier of $f_c = 1000 \text{ kHz}$.
- ② the f_{im} and its rejection ratio at a carrier of $f_c = 25 \text{ MHz}$.

Solution we have given $Q = 100$, $f_{if} = 455 \text{ kHz}$, $f_c = 1000 \text{ kHz}$.

$$\textcircled{1} f_{im} = f_c + 2f_{if} = 1000 + 2 \times 455 = 1910 \text{ kHz}.$$

$$\rho = \frac{f_{im}}{f_c} - \frac{f_c}{f_{im}} = \frac{1910}{1000} - \frac{1000}{1910} \approx 1.386$$

$$\text{For single tuned circuit } \alpha = \sqrt{1 + (Q\rho)^2} = \sqrt{1 + (100 \times 1.386)^2} = 138.6$$

$$\textcircled{2} f_c = 25 \text{ MHz}.$$

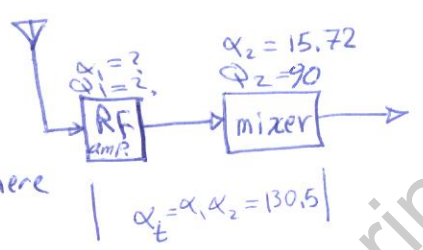
$$f_{im} = f_c + 2f_{if} = 25 + 2 \times 0.455 = 25.91 \text{ MHz}.$$

$$\rho = \frac{f_{im}}{f_c} - \frac{f_c}{f_{im}} \approx 0.0715$$

$$\therefore \alpha = \sqrt{1 + Q^2 \rho^2} = \sqrt{1 + (100 \times 0.0715)^2} = 5.22.$$

Hence, IRR is better at low frequencies i.e., the image frequency can be rejected better at low frequencies.

Q/ In order to make the Image frequency rejection of the receiver, which is superheterodyne AM receivers, good at high frequency, say, $f_c = 10 \text{ MHz}$, see Figure below, we need to add an RF amplifier with BPF. Calculate:



- ① The Quality factor of the RF-amplifier.
- ② If the RF-amplifier removed, what is the f_{IF} ? where $\rho = 1.45$.

Solution ① $Q_t = 130.5, f_c = 10 \text{ MHz}$

$$Q_t = Q_1 Q_2 = Q_1 \cdot 15.72 = 130.5 \Rightarrow Q_1 = 8.3 \Rightarrow f_{im} = 10 + 0.91 = 10.91 \text{ MHz}$$

$$Q_1 = \sqrt{1 + Q_1^2 \rho^2} \quad \rho = \frac{f_{im}}{f_c} - \frac{f_c}{f_{im}} = \frac{10.91}{10} - \frac{10}{10.91} = 0.1744$$

$$8.3^2 = 1 + Q_1^2 (0.1744)^2 \Rightarrow Q_1^2 = 2231.842 \Rightarrow Q_1 = 47.24$$

② Given $\rho = 1.45, f_c = 10 \text{ MHz}$

$$\rho = \frac{f_{im}}{f_c} - \frac{f_c}{f_{im}} \Rightarrow 1.45 = \frac{f_{im}}{10 \text{ MHz}} - \frac{10 \text{ MHz}}{f_{im}} = \frac{f_{im}^2 - 100 \times 10^{12}}{10 \times 10^6 f_{im}}$$

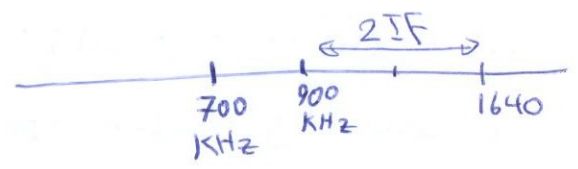
thus $f_{im} = 19.578 \text{ MHz}$

$$f_{im} = f_c + 2 f_{IF} = 10 \text{ MHz} + 2 f_{IF} = 19.578 \text{ MHz}$$

$$2 f_{IF} = 9.578 \text{ MHz} \Rightarrow f_{IF} = 4.789 \text{ MHz}$$

Q/ For a receiver with IF and RF frequencies of 455 KHz and 900 KHz respectively, determine the following:

- ① The local oscillator frequency.
- ② Image Frequency,
- ③ IFRR for a pre-selector Q of 80.



Solution

① $F_{LO} = f_c + f_{IF} = 900 + 455 = 1355 \text{ KHz}$

② $F_{im} = f_c + 2f_{IF} = 900 + 910 = 1810 \text{ KHz}$

③ IFRR :- $Q = 80$

$$\rho = \frac{f_{im}}{f_c} - \frac{f_c}{f_{im}} = \frac{1810}{900} - \frac{900}{1810} \approx 1.514$$

$$\alpha = \sqrt{1 + 6400(1.514)^2} = 121.114$$

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Q/ In a broadcast superheterodyne AM receiver having no RF section. The loaded Q factor of the serial coupling circuit (at the input of the mixer) is 125. IF the intermediate frequency is 465 kHz. Calculate:

- ① The image frequency and its rejection ratio at 1 MHz and 30 MHz.
- ② The IF-frequency required to make the image rejection ratio as good at 30 MHz as it is at 1 MHz.

Solution Given: $Q = 125$, $F_{IF} = 465 \text{ kHz}$, $F_{c1} = 1 \text{ MHz}$, $F_{c2} = 30 \text{ MHz}$.

① Consider

$$F_{c1} = 1 \text{ MHz} :-$$

$$f_{im} = f_c + 2f_{if} = 1000 + 2 \times 465 = 1930 \text{ kHz}$$

$$\rho = \frac{f_{im}}{f_c} - \frac{f_c}{f_{im}} = \frac{1930}{1000} - \frac{1000}{1930} = 1.93 - 0.518 = 1.4119$$

$$\alpha = \sqrt{1 + (125 \times 1.4119)^2} = 176.486 \text{ Better}$$

consider

$$F_{c2} = 30 \text{ MHz} \quad F_{im} = 30 + 2 \times 465 \text{ kHz} = 30 + 0.93 = 30.93 \text{ MHz}$$

$$\rho = \frac{30.93}{30} - \frac{30}{30.93} = 0.0611$$

$$\alpha = \sqrt{1 + (125 \times 0.0611)^2} = 7.699$$

② It is needed IRR $\alpha_n = 176.486$ @ $F_c = 30 \text{ MHz}$.

$$\rho = 1.4119 = \frac{f_{im}}{f_c} - \frac{f_c}{f_{im}} = \frac{f_{im}}{30 \text{ MHz}} - \frac{30 \text{ MHz}}{f_{im}}$$

$$f_{im} = 57 \text{ MHz}$$

$$f_{im} = F_c + 2f_{if} \Rightarrow 57 = 30 + 2f_{if}$$

$$\therefore F_{IF} = 13.5 \text{ MHz}$$

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